

# **Discussion 5:**

## **Trees, Mutation, and Nonlocal**

**Caroline Lemieux** (clemieux@berkeley.edu)

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# Administrativa

## Homeworks

HW 4 due tomorrow 3/1

## Projects

Maps due today!

## Events

Guerrilla Section Saturday 3/2 12-2PM, Soda 271

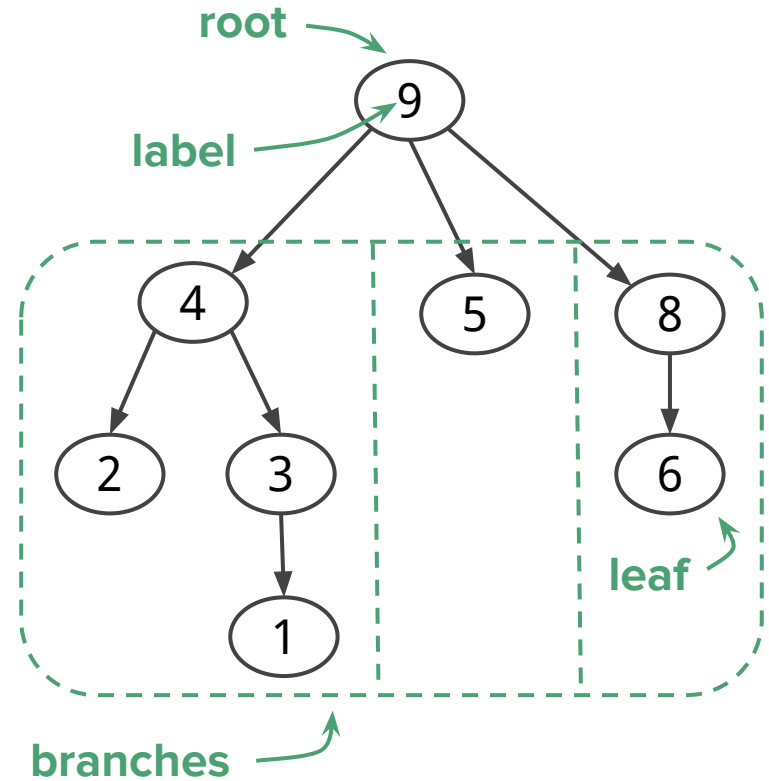
**Trees**

# Trees: Terminology

A **tree** is an ADT

**A tree's branches are individual trees themselves.**

Any confusing terminology on the first page of the discussion?



Trees: What you need to know

```
tree(label, branches)
```

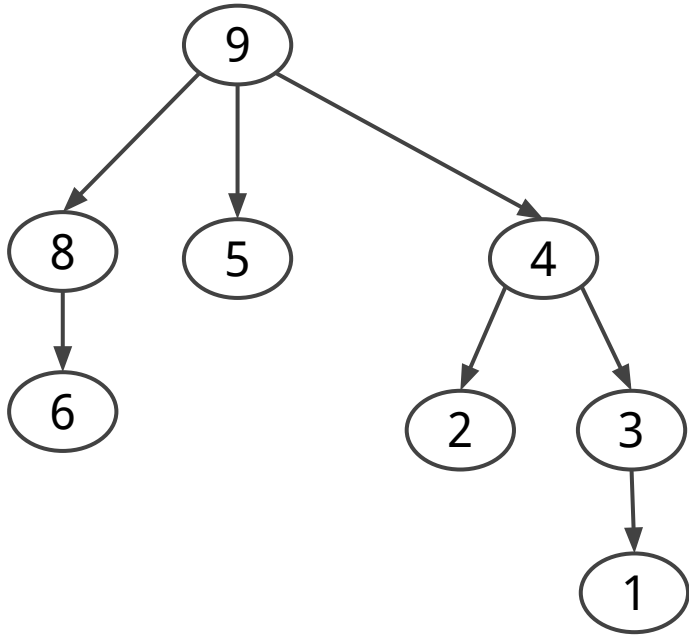
```
label(tree)
```

```
branches(tree)
```

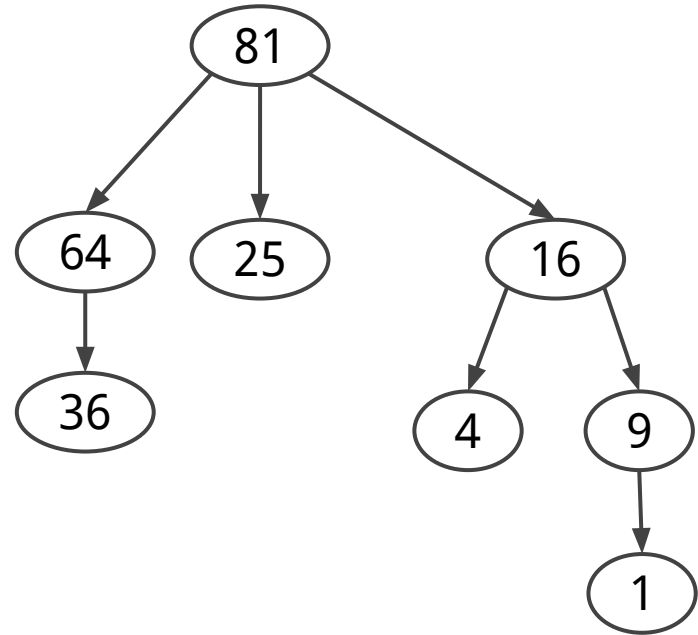
```
is_leaf(tree)
```

# Square Tree (1.2)

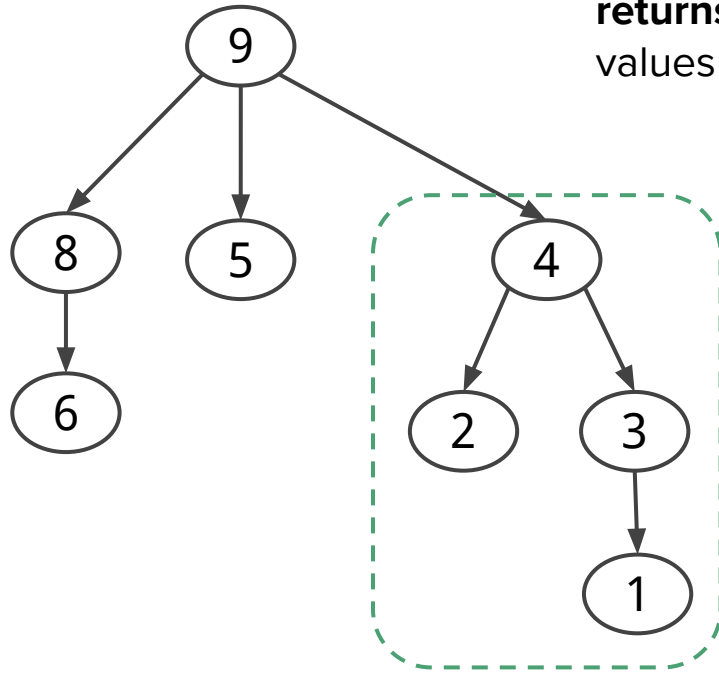
**Given:**



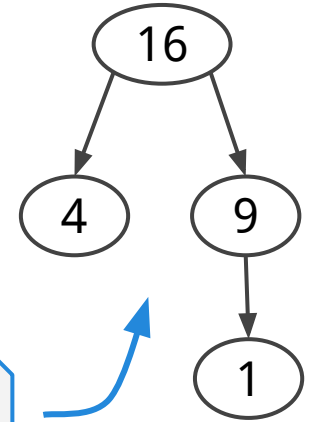
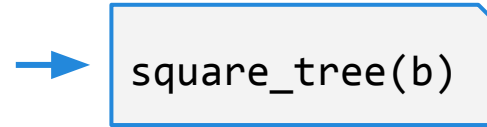
**Return:**



# Square Tree



A recursive call on a branch **returns a new tree** with the values of the branch squared.



# Square Tree

```
new_label = label(t) ** 2
```

```
new_branches = [square_tree(b) for b in branches(t)]
```

We combine this to get our solution:

```
def square_tree(t):  
    if is_leaf(t):  
        return tree(label(t) ** 2)  
    new_label = label(t) ** 2  
    new_branches = [square_tree(b) for b in branches(t)]  
    return tree(new_label, new_branches)
```



# Work on 1.1(height) and 1.3(tree\_max)!

Try 1.4 if you have time!

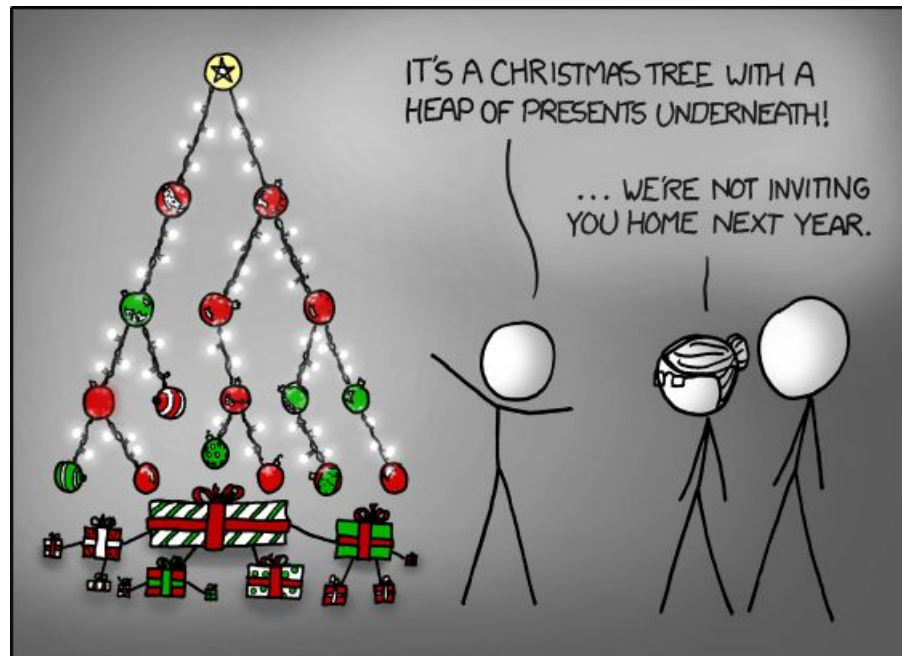
**Useful functions:**

`tree(label, branches)`

`label(tree)`

`branches(tree)`

`is_leaf(tree)`



# Work on 1.4(find\_path)



# Attendance




[links.cs61a.org/caro-disc](https://links.cs61a.org/caro-disc)

# List Mutation

# is vs ==

**is**: is the same thing in the box?

---

|   |         |
|---|---------|
| 1   | x = 3   |
|  | 2 y = 3 |

---

Global frame

|   |   |
|---|---|
| x | 3 |
| y | 3 |

**==**: are the things in the box equal

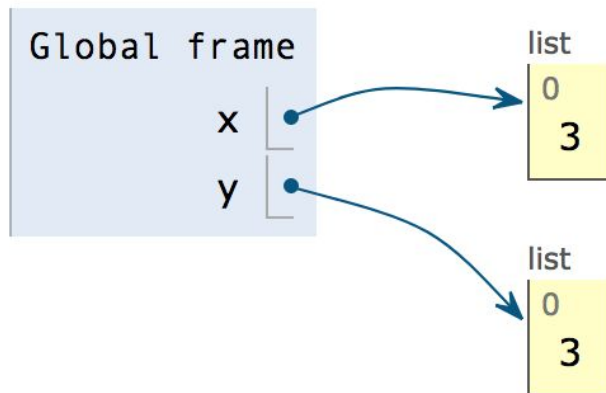
```
>>> x is y
True
>>> x == y
True
```

# is vs ==

**is**: is the same thing in the box?

**==**: are the things in the box equal

```
1 x = [3]
2 y = [3]
```

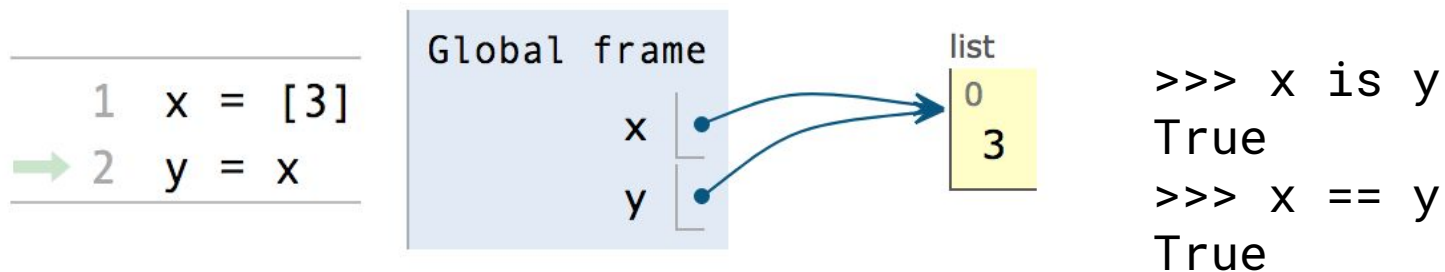


```
>>> x is y
False
>>> x == y
True
```

# is vs ==

**is**: is the same thing in the box?

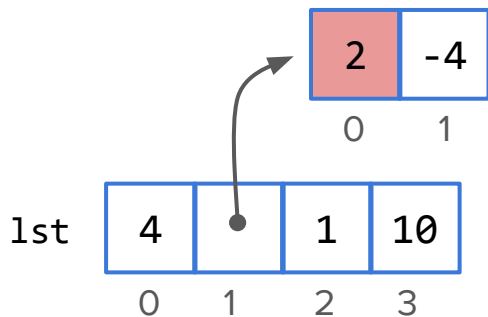
**==**: are the things in the box equal



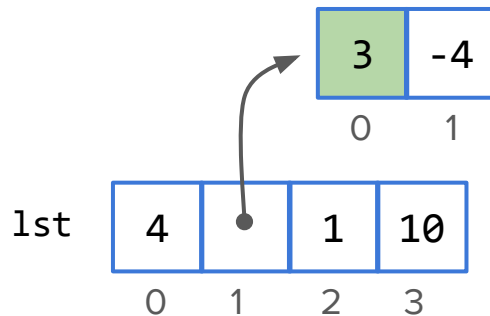
# Mutation

A list is a **mutable** object, meaning that we can modify its values!

We use **box-and-pointer diagrams** to keep track of the contents of a list.



```
lst[1][0] = 3
```

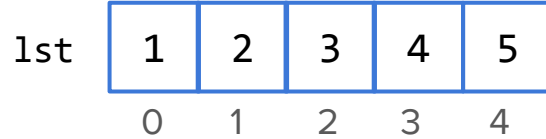




# append(e1)

Adds `e1` to the end of the list.

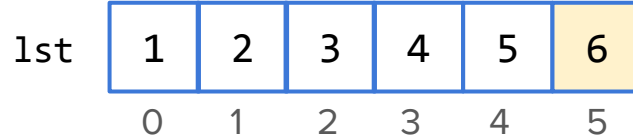
```
>>> lst = [1, 2, 3, 4, 5]
```



# append(e1)

Adds `e1` to the end of the list.

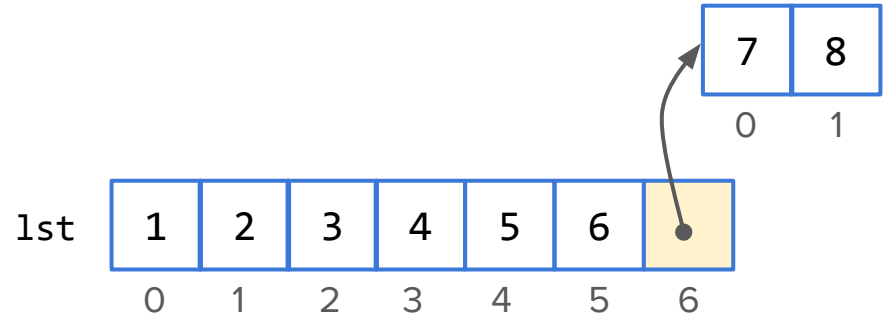
```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.append(6)
```



# append(e1)

Adds `e1` to the end of the list.

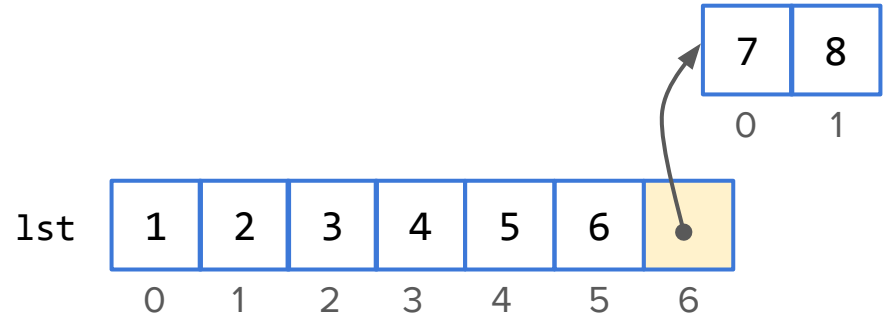
```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.append(6)
>>> lst.append([7, 8])
```



# append(e1)

Adds `e1` to the end of the list.

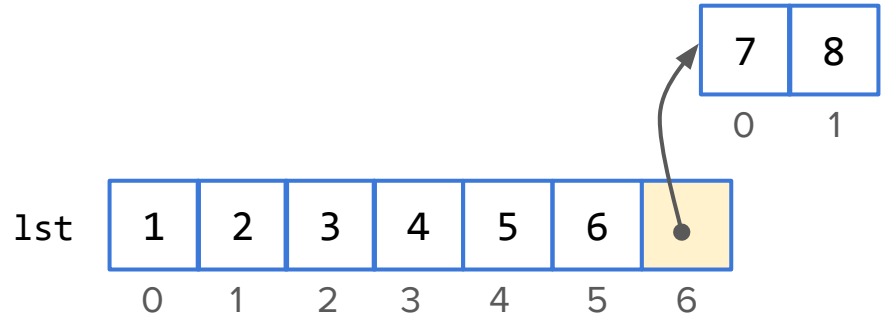
```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.append(6)
>>> lst.append([7, 8])
>>> lst
[1, 2, 3, 4, 5, 6, [7, 8]]
```



# append(el)

Adds `el` to the end of the list.

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.append(6)
>>> lst.append([7, 8])
>>> lst
[1, 2, 3, 4, 5, 6, [7, 8]]
```

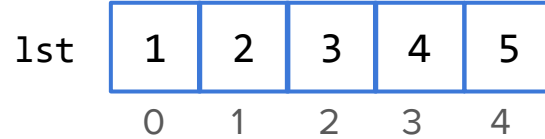


**Tip:** `append` adds a *single item* to the list. No matter what, you'll only have to draw one more box at the end of the list.

# extend(lst)

Concatenates `lst` to the end of the list.

```
>>> lst = [1, 2, 3, 4, 5]
```



# extend(lst)

Concatenates `lst` to the end of the list.

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.extend([6, 7, 8])
```



# extend(lst)

Concatenates `lst` to the end of the list.

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.extend([6, 7, 8])
>>> lst
[1, 2, 3, 4, 5, 6, 7, 8]
```





# extend(lst)

Concatenates `lst` to the end of the list.

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.extend([6, 7, 8])
>>> lst
[1, 2, 3, 4, 5, 6, 7, 8]
```

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.extend(6)
```


# extend(lst)

Concatenates `lst` to the end of the list.

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.extend([6, 7, 8])
>>> lst
[1, 2, 3, 4, 5, 6, 7, 8]
```

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.extend(6)
```

ERROR



extend must be given a *list*  
(or something else you can  
iterate through).

# extend(lst)

Concatenates `lst` to the end of the list.

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.extend([6, 7, 8])
>>> lst
[1, 2, 3, 4, 5, 6, 7, 8]
```



**Tip:** there are two ways to think about extend...

- Sticks a list at the end of the original
- Goes through `lst` one item at a time and appends each one

# WARNING: extend and +=

Extend does the **same thing** as `lst += [...]`, but is **different** from `lst = lst + [...]`.

```
>>> a = [1, 2, 3]
>>> b = a
>>> a += [4, 5]
>>> b
```

# WARNING: extend and +=

Extend does the **same thing** as `lst += [...]`, but is **different** from `lst = lst + [...]`.


```
>>> a = [1, 2, 3]
>>> b = a
>>> a += [4, 5]
>>> b
[1, 2, 3, 4, 5]
```

# WARNING: extend and +=

Extend does the **same thing** as `lst += [...]`, but is **different** from `lst = lst + [...]`.

```
>>> a = [1, 2, 3]
>>> b = a
>>> a += [4, 5]
>>> b
[1, 2, 3, 4, 5]
```

Same as  
`a.extend([4, 5])`




# WARNING: extend and +=

Extend does the **same thing** as `lst += [...]`, but is **different** from `lst = lst + [...]`.

```
>>> a = [1, 2, 3]
>>> b = a
>>> a += [4, 5]
>>> b
[1, 2, 3, 4, 5]
```

Same as  
`a.extend([4, 5])`




```
>>> a = [1, 2, 3]
>>> b = a
>>> a = a + [4, 5]
>>> b
[1, 2, 3]
```

# WARNING: extend and +=

Extend does the **same thing** as `lst += [...]`, but is **different** from `lst = lst + [...]`.


```
>>> a = [1, 2, 3]
>>> b = a
>>> a += [4, 5]
>>> b
[1, 2, 3, 4, 5]
```

Same as  
`a.extend([4, 5])`



```
>>> a = [1, 2, 3]
>>> b = a
>>> a = a + [4, 5]
>>> b
[1, 2, 3]
```

a now points to an entirely  
new list! The original was  
*not* mutated.

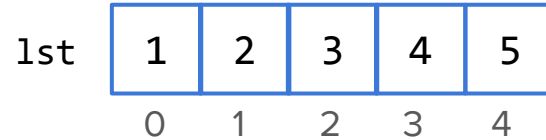




# insert(i, el)

Inserts `el` at index `i`, shifting the rest of the elements over.

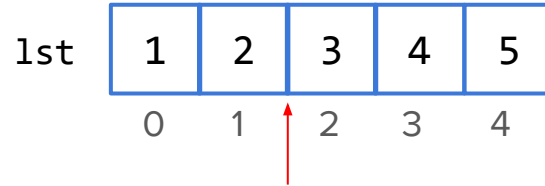
```
>>> lst = [1, 2, 3, 4, 5]
```



# insert(i, el)

Inserts `el` at index `i`, shifting the rest of the elements over.

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.insert(2, 9)
```

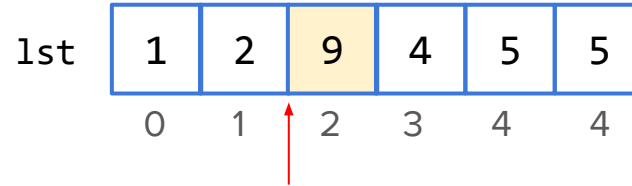


Item will be  
inserted at  
index 2...

# insert(i, el)

Inserts `el` at index `i`, shifting the rest of the elements over.

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.insert(2, 9)
```



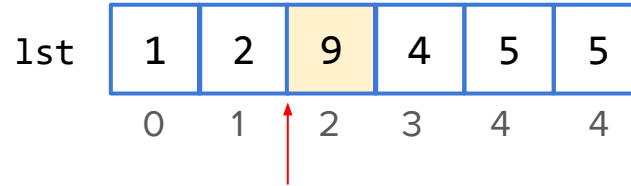
Item inserted  
at index 2...

rest of list shifted  
right to make  
room.

# insert(i, el)

Inserts `el` at index `i`, shifting the rest of the elements over.

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst.insert(2, 9)
>>> lst
[1, 2, 2.5, 3, 4, 5]
```



Item inserted  
at index 2...

rest of list shifted  
right to make  
room.

# Removing items

**remove(e1):** removes the first occurrence of `e1` from the list

```
>>> lst = [1, "oops", 3, 4, 5]
>>> lst.remove("oops")
>>> lst
[1, 3, 4, 5]
```

**pop(i):** removes and returns the element at index i

```
>>> lst = [1, 2, 3, 4, "hi"]
>>> lst.pop(3)
4
>>> lst.pop() # default: last item
"hi"
>>> lst
[1, 2, 3]
```

**NOTE:** **remove** takes an *item* to look for and delete.

**pop** takes an *index*, and returns the item that was deleted as a result.

# Check for Understanding

What does the following code display?

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst = lst.append(6)
>>> lst
```

- a. [1, 2, 3, 4, 5, 6]
- b. [1, 2, 3, 4, 5, [6]]
- c. Error
- d. None
- e. Nothing

# Check for Understanding

What does the following code display?

```
>>> lst = [1, 2, 3, 4, 5]
>>> lst = lst.append(6)
>>> lst
```

- a. [1, 2, 3, 4, 5, 6]
- b. [1, 2, 3, 4, 5, [6]]
- c. Error
- d. None
- e. **Nothing** ← `append` returns `None`, which interpreter doesn't display!

# Mutating a list vs. Creating a list

- `lst.append(element)`
  - `lst.extend(sequence)`
  - `lst.insert(index, element)`
  - `lst.remove(element)`
  - `lst.pop(index)`
  - `lst1 += lst2`
- Slicing
    - `lst[start:end:step]`
  - `lst1 = lst1 + lst2`

All of above except pop return **None**



# Work on 2.1

Draw box and pointer diagrams!!

# Work on 2.2

# **Nonlocal and Mutable Functions**

# Name lookup

x is found in local frame:

```
def foo():  
    x = 10  
    def bar(x):  
        return x  
    return bar
```

```
foo()(3)
```

x is found in parent frame:

```
def foo():  
    x = 10  
    def bar(y):  
        return x + y  
    return bar
```

```
foo()(3)
```

**Takeaway:** use binding in current frame if it exists and look in parent frames if it doesn't

# Assignment statements

Assigning a new variable in bar:

```
def foo():  
    x = 10  
    def bar():  
        x = 13  
        return x  
    return bar
```

```
foo()()
```

**Takeaway:** *Assignment statements create/modify new name bindings in the current frame; parent frames are uninvolved*

# Nonlocal

By default,

- you *can* **access** variables in parent frames.
- you *cannot* **modify** variables in parent frames.

**nonlocal** statements allow you to **modify** a name in a **parent** frame instead of creating a new binding in the current frame.

- cannot modify variables in current frame
- cannot create bindings in parent frames

```
def foo():  
    x = 10  
    def bar():  
        nonlocal x  
        x = 13  
    bar()  
    return x  
  
foo()
```

This **nonlocal** statement tells Python: “Don’t create a new local variable x; modify the one in the parent frame instead!”

# What does this mean?

- We can keep track of things across function calls!
  - Ex: count how many times a function was called, within the function itself
- Functions are not all pure anymore...could have **side effects** (!!!)
  - Could mess with things in other frames
  - Calling the same function twice may give different results
- We've covered all the cases for variable assignment now
  - Referencing variables in **local** and **parent** frames
  - Modifying variables in **local** and **parent** frames

# Warmup: WWPD?

```
def g(x):  
    def f():  
        x = 10  
        x = x + 2  
    f()  
    print(x)  
g(20)
```



# Warmup: WWPD?

```
def g(x):  
    def f():  
        x = 10  
        x = x + 2  
    f()  
    print(x)  
g(20)
```

**20**  
(local  
assignment  
doesn't change  
parent value)

# Warmup: WWPD?

```
def g(x):  
    def f():  
        x = 10  
        x = x + 2  
    f()  
    print(x)  
g(20)
```

**20**  
(local  
assignment  
doesn't change  
parent value)

```
def g(x):  
    def f():  
        x = 10  
        nonlocal x  
    f()  
    print(x)  
g(20)
```

# Warmup: WWPD?

```
def g(x):  
    def f():  
        x = 10  
        x = x + 2  
    f()  
    print(x)  
g(20)
```

**20**  
(local  
assignment  
doesn't change  
parent value)

```
def g(x):  
    def f():  
        x = 10  
        nonlocal x  
    f()  
    print(x)  
g(20)
```

**Error**  
(x is used  
before nonlocal  
declaration)

# Warmup: WWPD?

```
def g(x):  
    def f():  
        x = 10  
        x = x + 2  
    f()  
    print(x)  
g(20)
```

**20**  
(local  
assignment  
doesn't change  
parent value)

```
def g(x):  
    def f():  
        x = x - 8  
    f()  
    print(x)  
g(20)
```

```
def g(x):  
    def f():  
        x = 10  
        nonlocal x  
    f()  
    print(x)  
g(20)
```

**Error**  
(x is used  
before nonlocal  
declaration)

# Warmup: WWPD?

```
def g(x):  
    def f():  
        x = 10  
        x = x + 2  
    f()  
    print(x)  
g(20)
```

**20**  
(local  
assignment  
doesn't change  
parent value)

```
def g(x):  
    def f():  
        x = x - 8  
    f()  
    print(x)  
g(20)
```

**Error**  
(local var 'x'  
referenced  
before  
assignment)

```
def g(x):  
    def f():  
        x = 10  
        nonlocal x  
    f()  
    print(x)  
g(20)
```

**Error**  
(x is used  
before nonlocal  
declaration)

# Warmup: WWPD?

```
def g(x):  
    def f():  
        x = 10  
        x = x + 2  
    f()  
    print(x)  
g(20)
```

**20**  
(local  
assignment  
doesn't change  
parent value)

```
def g(x):  
    def f():  
        x = 10  
        nonlocal x  
    f()  
    print(x)  
g(20)
```

**Error**  
(x is used  
before nonlocal  
declaration)

```
def g(x):  
    def f():  
        x = x - 8  
    f()  
    print(x)  
g(20)
```

**Error**  
(local var 'x'  
referenced  
before  
assignment)

```
def g(x):  
    def f():  
        y = 5  
        nonlocal x  
        x = 10  
    f()  
    print(x)  
g(20)
```

# Warmup: WWPD?

```
def g(x):  
    def f():  
        x = 10  
        x = x + 2  
    f()  
    print(x)  
g(20)
```

**20**  
(local  
assignment  
doesn't change  
parent value)

```
def g(x):  
    def f():  
        x = 10  
        nonlocal x  
    f()  
    print(x)  
g(20)
```

**Error**  
(x is used  
before nonlocal  
declaration)

```
def g(x):  
    def f():  
        x = x - 8  
    f()  
    print(x)  
g(20)
```

**Error**  
(local var 'x'  
referenced  
before  
assignment)

```
def g(x):  
    def f():  
        y = 5  
        nonlocal x  
        x = 10  
    f()  
    print(x)  
g(20)
```

**10**  
(you can put  
'nonlocal'  
wherever you  
want, as long as  
it's before any  
references!)

# Warmup: WWPD?

```
def g(x):  
    def f(x):  
        nonlocal x  
        x = x + 2  
    f(1)  
    print(x)  
g(20)
```

## Error

'x' is both a parameter (local) and nonlocal. Python doesn't know which to use!



# General nonlocal rules

- Variable declared nonlocal must...
  - Be present in a parent frame
  - Not be in the global frame
  - Not have been declared locally in the current frame (either in the body or as a parameter)